

Infinite Geometric Series

Determine if each geometric series converges or diverges.

1) $a_1 = -3, r = 4$

2) $a_1 = 4, r = -\frac{3}{4}$

3) $a_1 = 5.5, r = 0.5$

4) $a_1 = -1, r = 3$

5) $81 + 27 + 9 + 3, \dots$

6) $7.1 + 17.75 + 44.375 + 110.9375, \dots$

7) $-3 + \frac{12}{5} - \frac{48}{25} + \frac{192}{125}, \dots$

8) $\frac{128}{3125} - \frac{64}{625} + \frac{32}{125} - \frac{16}{25}, \dots$

9) $\sum_{k=1}^{\infty} -4^{k-1}$

10) $\sum_{k=1}^{\infty} \frac{16}{9} \left(\frac{3}{2}\right)^{k-1}$

11) $\sum_{i=1}^{\infty} 4.2 \cdot 0.2^{i-1}$

12) $\sum_{k=1}^{\infty} \frac{7}{6} \left(-\frac{1}{4}\right)^{k-1}$

Evaluate each infinite geometric series described.

13) $a_1 = 3, r = -\frac{1}{5}$

14) $a_1 = 1, r = -4$

15) $a_1 = 1, r = -3$

16) $a_1 = 1, r = \frac{1}{2}$

17) $1 + 0.5 + 0.25 + 0.125\dots,$

18) $3 - \frac{9}{4} + \frac{27}{16} - \frac{81}{64}\dots,$

19) $81 - 27 + 9 - 3\dots,$

20) $1 - 0.6 + 0.36 - 0.216\dots,$

21) $\sum_{k=1}^{\infty} 5 \cdot \left(-\frac{1}{5}\right)^{k-1}$

22) $\sum_{n=1}^{\infty} -6 \cdot \left(-\frac{1}{2}\right)^{n-1}$

23) $\sum_{i=1}^{\infty} \left(\frac{1}{3}\right)^{i-1}$

24) $\sum_{k=1}^{\infty} 4^{k-1}$

Determine the common ratio of the infinite geometric series.

25) $a_1 = 1, S = 1.25$

26) $a_1 = 96, S = 64$

27) $a_1 = -4, S = -\frac{16}{5}$

28) $a_1 = 1, S = 2.5$

Infinite Geometric Series

Determine if each geometric series converges or diverges.

1) $a_1 = -3, r = 4$

Diverges

2) $a_1 = 4, r = -\frac{3}{4}$

Converges

3) $a_1 = 5.5, r = 0.5$

Converges

4) $a_1 = -1, r = 3$

Diverges

5) $81 + 27 + 9 + 3, \dots$

Converges

6) $7.1 + 17.75 + 44.375 + 110.9375, \dots$

Diverges

7) $-3 + \frac{12}{5} - \frac{48}{25} + \frac{192}{125}, \dots$

Converges

8) $\frac{128}{3125} - \frac{64}{625} + \frac{32}{125} - \frac{16}{25}, \dots$

Diverges

9) $\sum_{k=1}^{\infty} -4^{k-1}$

Diverges

10) $\sum_{k=1}^{\infty} \frac{16}{9} \left(\frac{3}{2}\right)^{k-1}$

Diverges

11) $\sum_{i=1}^{\infty} 4.2 \cdot 0.2^{i-1}$

Converges

12) $\sum_{k=1}^{\infty} \frac{7}{6} \left(-\frac{1}{4}\right)^{k-1}$

Converges

Evaluate each infinite geometric series described.

13) $a_1 = 3, r = -\frac{1}{5}$

 $\frac{5}{2}$

14) $a_1 = 1, r = -4$

No sum

15) $a_1 = 1, r = -3$

No sum

16) $a_1 = 1, r = \frac{1}{2}$

2

17) $1 + 0.5 + 0.25 + 0.125\dots,$

 2

18) $3 - \frac{9}{4} + \frac{27}{16} - \frac{81}{64}\dots,$

 $\frac{12}{7}$

19) $81 - 27 + 9 - 3\dots,$

 $\frac{243}{4}$

20) $1 - 0.6 + 0.36 - 0.216\dots,$

 0.625

21) $\sum_{k=1}^{\infty} 5 \cdot \left(-\frac{1}{5}\right)^{k-1}$

 $\frac{25}{6}$

22) $\sum_{n=1}^{\infty} -6 \cdot \left(-\frac{1}{2}\right)^{n-1}$

 -4

23) $\sum_{i=1}^{\infty} \left(\frac{1}{3}\right)^{i-1}$

 $\frac{3}{2}$

24) $\sum_{k=1}^{\infty} 4^{k-1}$

 No sum

Determine the common ratio of the infinite geometric series.

25) $a_1 = 1, S = 1.25$

 0.2

26) $a_1 = 96, S = 64$

 $-\frac{1}{2}$

27) $a_1 = -4, S = -\frac{16}{5}$

 $-\frac{1}{4}$

28) $a_1 = 1, S = 2.5$

 0.6