

Chapter 2 Polynomial and Rational Functions

Section 2.1 Quadratic Functions

Objective: In this lesson you learned how to sketch and analyze graphs of quadratic functions

Important Vocabulary		
Constant Function	Linear Function	Quadratic Function
Axis of Symmetry	Vertex	

I. The Graph of a Quadratic Function

Let n be a nonnegative integer and let $a_n, a_{n-1}, \dots, a_2, a_1, a_0$ be real numbers with $a_n \neq 0$. A **polynomial function of x with degree n** is given by:

$$f(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_2 x^2 + a_1 x + a_0$$

a_n is the expression
for the n^{th} coefficient

a_0 is the CONSTANT
TERM

What you should learn:

How to analyze graphs of
quadratic functions

A quadratic function is a polynomial function of SECOND degree. The graph of a quadratic function is a special "U-shaped" curved called a(n) PARABOLA.

If the leading coefficient of a quadratic function is positive, the graph of the function opens

UPWARD and the vertex of the parabola is the

MINIMUM point on the graph. If the leading coefficient of a quadratic function

is negative, the graph of the function opens DOWNWARD and the vertex of the

parabola is the maximum point on the graph.

II. The Standard Form of a Quadratic Function

The **standard form of a quadratic function** is

$$f(x) = a(x-h)^2 + k, a \neq 0$$

$(h, k) \rightarrow$ VERTEX of the
PARABOLA

What you should learn:

How to write quadratic
functions in standard form and
use the results to sketch the
graphs of functions

For a quadratic function in standard form, the axis (of symmetry) of the associated parabola is

$x=h$ and the vertex is (h,k) .

To write a quadratic function in standard form:

USE THE PROCESS OF COMPLETING THE SQUARE

To find the x-intercepts of the graph of $f(x) = ax^2 + bx + c$:

SOLVE THE EQUATION $ax^2 + bx + c = 0$

III. Finding Minimum and Maximum Values

For a quadratic function in the form $f(x) = ax^2 + bx + c$,

when $a > 0$, f has a minimum that occurs at

$-B/2A$. When $a < 0$, f has a maximum that

occurs at $-B/2A$.

To find the minimum or maximum value:

EVALUATE THE FUNCTION AT $-B/2A$

What you should learn:

How to find minimum and maximum values of quadratic functions in real-life applications

Section 2.1 Examples – Quadratic Functions

- (1) Describe the graph of $f(x) = 2x^2 + 8x + 8$ by identifying the vertex, axis of symmetry, x-intercepts, and direction the graph opens.

$f(x)$ opens upward

Vertex: $(-2, 0)$

A.o.S: $x = -2$

x-intercept: $(-2, 0)$

$$y = 2x^2 + 8x + 8$$

$$y - 8 = 2(x^2 + 4x)$$

$$y - 8 + 8 = 2(x^2 + 4x + 4)$$

$$y = 2(x + 2)^2$$

$$f(x) = 2(x + 2)^2$$

Completing
the square.

- (2) Write the standard form of the equation of the parabola whose vertex is $(1, 2)$ and that passes through the point $(3, -6)$.

x, y

$$y = a(x - h)^2 + k$$

$$-6 = a(3 - 1)^2 + 2$$

$$-6 = a(4) + 2$$

$$-8 = 4a$$

$$a = -2$$

$$y = -2(x - 1)^2 + 2$$