

Chapter 1 Functions and Their Graphs

Section 1.1 Lines in the Plane

Objective: In this lesson you will review how to find and use the slope of a line to write and graph linear equations

Important Vocabulary

Slope

Parallel

Perpendicular

I. The Slope of a Line

The formula for the **slope** of a line passing through the points (x_1, y_1) and (x_2, y_2) is $m = \frac{y_2 - y_1}{x_2 - x_1}$.

What you should learn:

How to find the slopes of lines

A line whose slope is positive rises from left to right.

A line whose slope is negative falls from left to right.

A line with zero slope is horizontal.

A line with undefined slope is vertical.

II. The Point-Slope Form of the Equation of a Line

The **point-slope** form of the equation of a line is

$$y - y_1 = m(x - x_1)$$

What you should learn:

How to write linear equations given points on lines and their slopes

This form of equation is best used to find the equation of a line when:

you are given slope and any point on the line

The **two-point form** of the equation of a line is $y - y_1 = \frac{y_2 - y_1}{x_2 - x_1}(x - x_1)$.

The two-point form of a line is best used to find the equation of a line when:

you are given any two points on the line
and no slope

A linear function has the form $f(x) = mx + B$. Its graph is a

Line that has slope m and a y-intercept at $(0, B)$.

III. Sketching Graphs of Lines

The slope-intercept form of the equation of a line is

$y = mx + B$, where m is the slope and the y-intercept is $(0, B)$.

What you should learn:

How to use slope-intercept forms of linear equations to sketch lines.

The equation of a horizontal line is $y = B$. The slope of a horizontal line is 0 . The y-coordinate of every point on the graph of a horizontal line is B .

The equation of a vertical line is $x = a$. The slope of a vertical line is undefined. The x-coordinate of every point on the graph of a vertical line is a .

The general form of the equation of a line is $Ax + By = C$.

might also be seen as $Ax + By + C = 0$

Every line has an equation that can be written in

general form (Standard form).

IV. Parallel and Perpendicular Lines

The relationship between the slope of two lines that are

parallel is: They are equal

$$m_1 = m_2$$

What you should learn:

How to use slope to identify parallel and perpendicular lines

The relationship between the slope of two lines that are perpendicular is:

they are opposite reciprocals.

$$m_1 = -\frac{1}{m_2}$$

opposite reciprocal

this works just as well too
 $m_1 \times m_2 = -1$

A line that is parallel to a line whose slope is 2 has a slope of 2.

A line that is perpendicular to a line whose slope is 2 has a slope of $-\frac{1}{2}$.

Section 1.1 Examples – Lines in the Plane

- (1) Find the point-slope form of the equation that passes through the given point and has the indicated slope.

$$(-3, 6)$$

$$m = -2$$

$$y - y_1 = m(x - x_1)$$

$$y - 6 = -2(x + 3)$$

- (2) Decide whether the two lines are *parallel*, *perpendicular*, or *neither*.

$$y = 4x - 1$$

$$2x + 8y = 12$$

$$m_1 = 4$$

$$8y = -2x + 12$$

$$y = -\frac{1}{4}x + \frac{3}{2}$$

$$m_2 = -\frac{1}{4}$$

Perpendicular

- (3) Determine the slope and y-intercept (if possible) of the linear equation.

$$3x + 4y = 1$$

$$4y = -3x + 1$$

$$y = -\frac{3}{4}x + \frac{1}{4}$$

$$m = -\frac{3}{4}$$
$$y\text{-int: } (0, \frac{1}{4})$$

← This is a location (a point); therefore, it must have an x- and y-value in the answer